# Analytical Algorithms for Synthesis of the State Space Controllers for the Control Systems with Aperiodic Step Response

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Abstract — Elaboration of the analytical algorithms for synthesis of the state space controllers, in form of algebraic expressions, by the maximum stability degree criterion, that offers to the designed control systems an aperiodic step response, high performance and good robustness is proposed in this paper. The elaborated algorithms represent simple analytical procedures with reduced volume of calculation and without any imposing conditions to the complexity of the control object.

Keywords — control system; state space representation; synthesis of the state space controllers; analytical algorithms; maximum stability degree; aperiodic step response

### I. INTRODUCTION

State space representation has become the mathematical support in the systems theory and a source for a new series of approaches and modern methods for analysis and synthesis of control systems. This fact is due to the following issues: representation in the state space using the matrix calculations that are easy to implement on the computer; permits unitary treatment of the mono-variable and multi-variable systems, continuous and discrete systems, linear and nonlinear systems; it is used for synthesis of the controllers to the higher order objects etc. The state variables  $x(t) = [x_1(t), x_2(t), \dots, x_n(t)]$  are those variables that determine the future behavior of the system, when the initial state of the system and the inputs are known. For state space realization of the system it is need to be satisfied the condition of controllability and observability [1, 2, 5, 6].

Synthesis of the state space controller is started with determination of the characteristic polynomial  $\varphi_A(p)$  of the control system state matrix A, imposing the poles (proper values)  $[\gamma_1, \gamma_2, ..., \gamma_n]$ , that determine the desired dynamics of the design system, according to which is obtained the characteristic polynomial  $\varphi_c(p)$  of the system matrix in the closed loop. For determination of the feedback vector' components k (tuning parameters) is used the Ackermann relation [2, 5, 7]

$$k = [0 \ 0 \ \dots \ 1] U^{-1} \varphi(A) =$$
  
= [0 \ 0 \ \... 1] [B, AB, \..., A^{n-1}B]^{-1} \varphi(A) (1,a)

where  $\varphi(A) = A^n + q_{n-1}A^{n-1} + \dots + q_1A + q_0I$ ; U - the controllability matrix.

In case of presentation of the system in canonical controllability form, calculation of the feedback vector' components is reduced to use the following expressions [5, 6]

$$k_i = q_i - \alpha_i, \ i = 0, ..., (n-1),$$
 (1,b)

where  $q_i$  and  $\alpha_i$  represent the coefficients of characteristic polynomials  $\varphi_c(p)$  and  $\varphi_A(p)$  respectively.

Thus, using the feedback by the state is possible to modify all poles of the control system and, therefore, imposing the dynamic behavior according to the desired performance by choosing the proper values of the system matrix in the closed loop. The choosing of new proper values is a complex problem and using of classical methods of synthesis, for example, the dominant poles method, the responses prototype method, the analytical design of controllers etc., for the control systems with high order is met difficulties that appears in case of correlation the poles of the system with the desired performance and energetic indices, required the graphic design, using the computer and obtained the optimal parameters by these methods sometimes can not satisfy the condition of stability.

In [3] is proposed a new synthesis method of the controller in the state space by the maximum stability degree criterion (MSD), criterion that offers to the design systems the higher performance and better robustness [4].

The problem of synthesis the control system in the state space with maximum stability degree is formulated in the following way [3]. It is considered a structure of mono-variable control system with representation in the state space (Fig.1), that includes the control object with known parameters

$$\begin{cases} \dot{x} = Ax + bu, \\ y = c^T x, \end{cases}$$
(2)

and control algorithm

$$u(t) = -k^T x(t) = -[k_0 \quad k_1 \quad \cdots \quad k_{n-1}] \cdot [x_1 \quad x_2 \quad \dots \quad x_n]^T, \quad (3)$$

where A is the state matrix with dimension  $(n \times n)$ ; x the vector of the state variables,  $(n \times 1)$ ; u - the control value; b - the vector of control values,  $(n \times 1)$ ; c - the vector of output values,  $(n \times 1)$ ; k - the vector of tuning parameters,  $(n \times 1)$ ; n - the order of the system; y - the output value.



Fig. 1. The block scheme of a dynamic system in the state space.

It is necessary to determine the components of the feedback vector (tuning parameters), so as to be satisfied the condition

$$J = \max_{k_i} \eta(k_i), i = (1, ..., n),$$
(4)

where J is the maximum stability degree;  $\eta$  - the stability degree of the system;  $k_i$  - the components of the tuning parameters vector; n - the degree of the characteristic polynomial of the control system.

In conformity with method [3], it is introduced the notion of the maximum stability degree J and using the substitution  $p_i = -J \pm j\omega_k$ , the desired characteristic polynomial  $\varphi_c(p)$  of the design system is obtained by the decomposition of the characteristic polynomial  $\varphi_A(p)$  of the A matrix in n linear factors

$$\varphi_{c}(p) = \prod_{k=1}^{l} (p - j\omega_{k} + J)(p + j\omega_{k} + J) \prod_{j=1}^{z} (p + J) = (5)$$
$$= p^{n} + q_{n-1}p^{n-1} + \dots + q_{1}p + q_{0},$$

where *l* is the number of conjugate pairs of complex roots; *z* - the number of real roots; n = 2l + z - the degree of the characteristic polynomial of the design control system;  $q_i = f_i(J, \omega_k), i = (0, ..., n-1)$ .

The value of the maximum stability degree J of the designed control system is obtained from the following expression [3]

$$J = \frac{\alpha_{n-1}}{n},\tag{6}$$

where  $\alpha_{n-1}$  is a coefficient of the characteristic polynomial  $\varphi_4(p)$ .

The values of the tuning parameters  $k_i$  are determined in conformity with expressions (1, b).

The practice of synthesis the controllers demonstrates, however, that for determination of the dynamic tuning parameters of the controller is more convenient to operate with the analytical expressions with a low volume of calculations that dependent on the known parameters of control object. The analytical synthesis expressions, on the one hand have the advantage of decreasing the volume of calculation of tuning parameters (compared with the synthesis methods and algorithms that include a number of steps) and, by the other hand, using of the analytical expressions is a good alternative in case of the controllers with auto-tuning and in adaptive control, where the controller retuning is done in function of the parameters variation of the control object during operation of the control system.

Based on this consideration, in this paper is proposed to elaborate of the analytical algorithms of synthesis the state space controllers, in form of algebraic expressions, for control objects with arbitrary order inertia by the maximum stability degree criterion.

## II. ANALYTICAL ALGORITHMS FOR SYNTHESIS OF THE STATE SPACE CONTROLLERS

If it is imposed the problem to design of the control system in the state space by the error, the solution of this problem depends on the structure of control system, where the control object can be with inertia and astatism.

The transfer function of control object with inertia is given in the following form:

$$H_F(s) = \frac{k}{a_0 s^n + a_1 s^{n-1} + \dots + a_{n-1} s + a_n},$$
(7)

where k is the transfer coefficient;  $a_0, a_1, ..., a_n$  - the coefficients of the transfer function of control object, n - the order of control object. For the control object with inertia and astatism we have the coefficient  $a_n = 0$ .

The standard controllable form of representation in the state space of the object (7), normalized by the  $a_0$ , is

$$\begin{bmatrix} \dot{x}_{1} \\ \dot{x}_{2} \\ \vdots \\ \dot{x}_{n-1} \\ \dot{x}_{n} \end{bmatrix} = \begin{bmatrix} 0 & 1 & \cdots & 0 & 0 \\ 0 & 0 & \cdots & 0 & 0 \\ \vdots & \vdots & \ddots & \vdots & \vdots \\ 0 & 0 & \cdots & 0 & 1 \\ -\alpha_{0} & -\alpha_{1} & \cdots & -\alpha_{n-2} & -\alpha_{n-1} \end{bmatrix} \begin{bmatrix} x_{1} \\ x_{2} \\ \vdots \\ x_{n-1} \\ x_{n} \end{bmatrix} + \begin{bmatrix} 0 \\ 0 \\ \vdots \\ 0 \\ 1 \end{bmatrix} u,$$
(8)  
$$y = [\beta_{0} & 0 & 0 & \dots & 0]x = \beta_{0}x_{1}.$$

where 
$$\alpha_0 = \frac{a_n}{a_0}; \alpha_1 = \frac{a_{n-1}}{a_0}; ...; \alpha_{n-1} = \frac{a_1}{a_0}; \beta_0 = \frac{k}{a_0}.$$

To the model object with inertia and astatism in expression (8) we have  $\alpha_0 = 0$ .

For the control object with inertia and astatism the structural block scheme of the control system in the state space is represented in the Fig. 2 [2]. To amplify the error signal, in direct connection is included the proportional block  $k_0$ . The control algorithm is determined by the following expression

$$u(t) = -[k_1 \quad k_2 \quad \cdots \quad k_{n-1}] \cdot [x_2 \quad x_3 \quad \dots \quad x_n]^T + k_0 \varepsilon .$$
(9)

If at the entrance of the control system with object with inertia is applied the step signal, then to obtain the sta-



Fig. 2. The structural block scheme of the control system for the object with inertia and astatism.

tionary error null is necessary to add in the controller structure an integrator element, which increase the order of the designed system (Fig. 3) [2]. The control algorithm, in this case, is determined by the following expression

$$u(t) = -\begin{bmatrix} k_1 & k_2 & \cdots & k_n \end{bmatrix} \cdot \begin{bmatrix} x_1 & x_2 & \cdots & x_n \end{bmatrix}^T + k_0 \varepsilon .$$
(10)

The characteristic polynomial of the state matrix of the control system (Fig. 2, 3) is presented:

• for the objects with inertia and astatism (Fig. 2)

$$p_A(p) = p^n + \alpha_{n-1}p^{n-1} + \dots + \alpha_1p;$$
 (11, a)

• for the object with inertia (Fig. 3)

$$\varphi_{\hat{A}}(p) = p^{n+1} + \alpha_{n-1}p^n + \dots + \alpha_1 p^2 + \alpha_0 p . \quad (11, b)$$

The step response of control system will be aperiodic, if the imaginary parts of the characteristic polynomial roots are null. Therefore, in accordance with the method [3], it is introduced the notion of the maximum stability degree J and considering the roots of the characteristic polynomial  $p_i = -J$ , it forms the desired characteristic polynomial  $\varphi_c(p)$  by decomposing polynomial (11) in the linear factors:

• for the model objects with inertia and astatism

$$\begin{aligned} \varphi_c(p) &= (p+J)^n = c_n p^n + c_{n-1} J p^{n-1} + \\ &+ c_{n-2} J^2 p^{n-2} + \ldots + c_1 J^{n-1} p + c_0 J^n = \\ &= q_n p^n + q_{n-1} p^{n-1} + q_{n-2} p^{n-2} + \ldots + q_1 p + q_0 \,, \end{aligned}$$
 (12, a)

where  $q_i = f_i(c_i, J)$ , i = (0, ..., n) and value of the maximum stability degree J of the design system is determined by the following expression

$$I = \frac{\alpha_{n-1}}{n}; \qquad (13, a)$$

• for the model objects with inertia

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$$\begin{split} \varphi_c(p) &= (p+J)^{n+1} = c_{n+1}p^{n+1} + c_nJp^n + \\ &+ c_{n-1}J^2p^{n-1} + \ldots + c_1J^np + c_0J^{n+1} = \\ &= q_{n+1}p^{n+1} + q_np^n + q_{n-1}p^{n-1} + \ldots + q_1p + q_0 \,, \end{split} \tag{12, b}$$

where  $q_i = f_i(c_i, J), i = (0, ..., (n+1));$   $q_i = f_i(c_i, J),$ i = (0, ..., n) and the value of stability degree is

$$J = \frac{\alpha_{n-1}}{n+1} \,. \tag{13, b}$$

From the characteristic polynomials  $\varphi_A(p)$  (11, *a*),  $\varphi_c(p)$  (12, *a*) and relations (13, *a*), (1, *b*) for the objects with inertia and astatism is obtained

$$J = \frac{\alpha_{n-1}}{n}, \ k_0 = q_0 / \beta_0; \ k_i = q_i - \alpha_i, \ i = 1, ..., (n-1) \ (14, a)$$

or from  $\varphi_{\hat{A}}(p)$  (11, b),  $\varphi_c(p)$  (12, b) and relations (13,b), (1, b) for the model objects with inertia is obtained

$$J = \frac{\alpha_{n-1}}{n+1}, \ k_0 = q_0 / \beta_0; \ k_i = q_i - \alpha_{i-1}, \ i = (1,...,n) . \ (14, b)$$

Using the relations (14) the maximum stability degree J and the tuning parameters  $k_i$  of the state space controller can be calculated.

The expressions (12, a, b)

$$(p+J)^{n} = c_{n}p^{n} + c_{n-1}Jp^{n-1} + c_{n-2}J^{2}p^{n-2} + \dots + c_{1}J^{n-1}p + c_{0}J^{n}$$
(15, a)

$$(p+J)^{n+1} = c_{n+1}p^{n+1} + c_nJp^n + c_{n-1}J^2p^{n-1} + \dots + c_1J^np + c_0J^{n+1}$$
(15, b)

represent the Newton binomial and their coefficients are calculated by the following expressions [8]



Fig. 3. The structural block scheme of the control system for the object with inertia.

$$c_{0} = 1, c_{i} = c_{n}^{i} = \frac{n(n-1)\dots(n-i+1)}{1 \cdot 2\dots i} = \prod_{\substack{l=1\\i!}}^{i} (n-l+1) = \frac{n!}{i!(n-i)!}, i = (1,\dots,n)$$
(16)

where for the (15, *a*) have  $c_i = c_n^i$  and for the (15, *b*) -  $c_i = c_{n+1}^i$ .

Using the expressions (14) and expression for calculation of the binomial coefficients (16) and taking into account the order of the closed loop system (for the control object with inertia and astatism is n, but for the control object with inertia is (n+1)), after some transformations were elaborated the analytical algorithms of synthesis the state space controllers, in form of algebraic expressions, for the control object with arbitrary order inertia n and with or without astatism for the control system with maximum stability degree and aperiodic step response. The elaborated algorithms are presented in the Tables I and II.

TABLE I. THE ANALYTICAL ALGORITHMS FOR SYNTHESIS OF THE STATE SPACE CONTROLLERS TO THE OBJECTS WITH INERTIA AND ASTATISM

No.	The calculation expressions						
1	Transfer function of the control object $H_F(s) = \frac{k}{a_0 s^n + a_1 s^{n-1} + a_2 s^{n-2} + \dots + a_{n-2} s^2 + a_{n-1} s}$						
2	Normalized transfer function $H_F(s) = \frac{\beta_0}{s^n + \alpha_{n-1}s^{n-1} + \alpha_{n-2}s^{n-2} + \dots + \alpha_2s^2 + \alpha_1s},$ $\alpha_1 = \frac{a_{n-1}}{a_0}; \dots, \alpha_{n-2} = \frac{a_2}{a_0}; \alpha_{n-1} = \frac{a_1}{a_0}; \beta_0 = \frac{k}{a_0}.$						
3	$\begin{bmatrix} \dot{x}_{1} \\ \dot{x}_{2} \\ \vdots \\ \dot{x}_{n-1} \\ \dot{x}_{n} \end{bmatrix} = \begin{bmatrix} 0 & 1 & \cdots & 0 & 0 \\ 0 & 0 & \cdots & 0 & 0 \\ \vdots & \vdots & \ddots & \vdots & \vdots \\ 0 & 0 & \cdots & 0 & 1 \\ 0 & -\alpha_{1} & \cdots & -\alpha_{n-2} & -\alpha_{n-1} \end{bmatrix} \begin{bmatrix} x_{1} \\ x_{2} \\ \vdots \\ x_{n-1} \\ x_{n} \end{bmatrix} + \begin{bmatrix} 0 \\ 0 \\ \vdots \\ 0 \\ 1 \end{bmatrix} u,$ $y = [\beta_{0}  0  0  \dots  0]x.$						
4	Controllability condition $rangU = rang[b \ Ab \ A^2b \ A^3b \ A^{n-1}b] = n$						
5	$\label{eq:control low} \begin{split} & \text{Control low} \\ u = -[k_1,k_2,k_3,,k_{n-1}] \cdot [x_2,x_3,x_4,,x_n]^T + k_0 \varepsilon \;. \end{split}$						
6	Determination of the maximum stability degree and the coefficients of tuning parameters vector $J = \frac{\alpha_{n-1}}{n} = \frac{a_1}{na_0},$ $k_0 = \frac{J^n}{\beta_0}, \ k_i = \frac{\prod_{l=1}^{i} (n-l+1)}{i!} J^{n-i} - \alpha_i, \ i = 1,, (n-1)$						

TABLE II. THE ANALYTICAL ALGORITHMS FOR SYNTHESIS OF THE STATE SPACE CONTROLLERS TO THE OBJECTS WITH INERTIA



#### **III. APPLICATIONS AND COMPUTER SIMULATION**

Suppose that the controlled technological process is described by the model object with fourth order inertia with known parameters

$$H_F(s) = \frac{6}{(0,5s+1)(s+1)(2s+1)(4s+1)} = \frac{6}{4s^4 + 15s^3 + 17,5s^2 + 7,5s+1},$$
(17)

where k = 6,  $a_0 = 4, a_1 = 15, a_2 = 17, 5, a_3 = 7, 5, a_4 = 1$ .

It is formulated the problem to synthesis of the controller in the state space to the model object (17) and to determine the vector of tuning parameters k.

It is obtained the normalized transfer function by the  $a_0$ 

$$\begin{split} H_F(s) &= \frac{\beta_0}{s^4 + \alpha_3 s^3 + \alpha_2 s^2 + \alpha_1 s + \alpha_0} = \\ &= \frac{1,5}{s^4 + 3,75s^3 + 4,375s^2 + 1,875s + 0,25}, \end{split}$$

where  $\alpha_0 = \frac{a_4}{a_0} = 0,25; \alpha_1 = \frac{a_3}{a_0} = 1,875; \alpha_2 = \frac{a_2}{a_0} = 4,375;$  $\alpha_3 = \frac{a_1}{a_0} = 3,75; \beta_0 = \frac{k}{a_0} = 1,5.$ 

It is determined the vector-matrix equation in the standard controllable realization

$$\begin{vmatrix} \dot{x}_1 \\ \dot{x}_2 \\ \dot{x}_3 \\ \dot{x}_4 \end{vmatrix} = \begin{bmatrix} 0 & 1 & 0 & 0 \\ 0 & 0 & 1 & 0 \\ 0 & 0 & 0 & 1 \\ -0,25 & -1,875 & -4,375 & -3,75 \end{bmatrix} \begin{bmatrix} x_1 \\ x_2 \\ x_3 \\ x_4 \end{bmatrix} + \begin{bmatrix} 0 \\ 0 \\ 0 \\ 1 \end{bmatrix} u,$$

The stationary error of the control system will be null if in the structure of controller is connected an integrator element (Fig. 3), which raises the order of the designed system and the above equation is transformed in the following form [2, 6]

$$\begin{bmatrix} \dot{x}_1 \\ \dot{x}_2 \\ \dot{x}_3 \\ \dot{x}_4 \\ \dot{\varepsilon} \end{bmatrix} = \begin{bmatrix} 0 & 1 & 0 & 0 & 0 \\ 0 & 0 & 1 & 0 & 0 \\ 0 & 0 & 0 & 1 & 0 \\ -0.25 & -1.875 & -4.375 & -3.75 & 0 \\ -1.5 & 0 & 0 & 0 & 0 \end{bmatrix} \cdot \begin{bmatrix} x_1 \\ x_2 \\ x_3 \\ x_4 \\ \varepsilon \end{bmatrix} + \\ + \begin{bmatrix} 0 \\ 0 \\ 0 \\ 1 \\ 0 \end{bmatrix} u + \begin{bmatrix} 0 \\ 0 \\ 0 \\ 1 \\ 0 \end{bmatrix} r, \\ y = \begin{bmatrix} 1, 5 & 0 & 0 & 0 \end{bmatrix} r.$$

It is obtained the characteristic polynomial of the  $\hat{A}$  matrix

$$\varphi_{\hat{A}}(p) = p^5 + 3,75p^4 + 4,375p^3 + 1,875p^2 + 0,25p = = p^5 + \alpha_3 p^4 + \alpha_2 p^3 + \alpha_1 p^2 + \alpha_0 p$$

It is verified the condition of controllability of the system

$$angU = rang[\hat{b}, \hat{A}\hat{b}, \hat{A}^2\hat{b}, \hat{A}^3\hat{b}, \hat{A}^4\hat{b}] = 5.$$

Because the rank of matrix U is equal with order of the system, then the system is controllable.

In conformity with (10) the control algorithm is presented in the following form

$$u(t) = -[k_1, k_2, k_3, k_4] \cdot [x_1, x_2, x_3, x_4]^T + k_0 \varepsilon.$$

The synthesis of controller by the maximum stability degree criterion is done based on analytical algorithms, presented in the Table II.

$$J = \frac{\alpha_3}{5} = \frac{a_1}{5a_0}, k_0 = \frac{J^5}{\beta_0}, k_1 = 5J^4 - \alpha_0,$$
  
$$k_2 = 10J^3 - \alpha_1, k_3 = 10J^2 - \alpha_2, k_4 = 5J - \alpha_3$$

The results of synthesis are given in the Table III.

Using the method of dominant poles for the system with imposed indices of performance  $\sigma < 5\%$ ,  $t_r < 10s$ , it is determined the dominates poles [2]:

$$\circ \quad \sigma < 5\% \implies \psi \approx 1;$$
  
$$\circ \quad t_r < 10 s \implies 10 \approx \frac{3}{\psi \omega_n} \implies \eta = \psi \omega_n = 0,3$$

where  $\omega_n$  is a proper frequency;

• in final is choice  $\gamma_{1,2} = p_{dom} = -0.3$ , which allows to impose the other poles  $\gamma_{3.4.5} = -1$ .

The characteristic polynomial of the designed control system is determined

$$\begin{aligned} \varphi_c(p) &= (p+0,3)^2(p+1)^3 = \\ &= p^5 + 3.6 p^4 + 4.89 p^3 + 3.07 p^2 + 0.87 p + 0.09 = \\ &= p^5 + q_4 p^4 + q_3 p^3 + q_2 p^2 + q_1 p + q_0. \end{aligned}$$

Using the relation (14, b) is determined the vector of tuning parameters k, which values are presented in the Table III.

To calculate the tuning parameters by the parametric optimization method was used the Matlab Simulink software (the simulation structural block scheme of the control system in the state space is presented in the Fig. 4) and the obtained results are presented in the Table III.

TABLE III. THE RESULTS OF SYNTHESIS THE CONTROLLER

No.	The syn- thesis methods	$k_0$	$k_1$	$k_2$	$k_3$	$k_4$	
1	Maximum	J=0,75					
	stability degree	0,158	1,33	2,344	1,25	0	
2	The domi- nation poles	0,06	0,62	1,195	0,515	-0,15	
3	Parametrical optimization	0,091	0,538	0,257	-0,962	-0,915	



Fig. 4. The simulation structural block scheme of the control system in the state space.

The step responses of the designed control system are presented in the Fig. 5 and the performance are given in the Table IV ( $\varepsilon_{st} = \pm 5\%$  from  $y_{st}$ ). The numbering of curves correspond to the numbering of the methods in the Table III.



Fig.5. The step responses of the designed control system.

TABLE IV. The Performance of the Designed Control System

No.	The synthesis	The performance of control system					
	method	$t_c, s$	$t_r, s$	σ, %	λ	ψ	
1	Maximum stability degree	8,95	12,2	-	-	-	
2	The domination poles	15	19,2	-	-	-	
3	Parametrical optimization	5,6	12,6	5,5	1	1	

# **IV.** CONCLUSIONS

1. Based on the theoretical investigations were developed the analytical algorithms for synthesis of the state space controllers, in form of algebraic expressions, for designing the control systems by the maximum stability degree criterion.

2. The elaborated algorithms represent the simple analytical procedures with a low volume of calculations, that not impose the restrictions on the complexity of control objects and can be applied for different types of objects: with inertia of arbitrary order; inertia and astatism; inertia and time delay; inertia, astatism and time delay.

3. Application of elaborated analytical algorithms simplify the synthesis procedure of the state space controllers, which provides the necessary conditions for implementation the control systems with auto-tuning and adaptive control, and enable the development of computeraided design of control systems.

4. Analyzing the performance of the designed control system by the proposed analytical algorithms for synthesis of the state space controller, in comparison with parametrical optimization and dominant poles methods, was noticed that elaborated algorithms offers to the designed control systems the aperiodic step response, higher performance and better robustness.

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